Data Mining Tasks

- Classification
- Prediction
- Clustering
- Dependency Modelling
- Summarization
- Change and Deviation Detection
- Visualization

Data Mining Tasks 1

• prediction of a (future) category based on observed data

ullet prediction of a (future) category based on observed data ightarrowclassification

- \bullet prediction of a (future) category based on observed data \rightarrow
- prediction of a (future) numerical value y based on observed data \vec{x}
 - y: response output, dependent variable
 - \vec{x} : input, regressors, explanatory variables, independent variables

- prediction of a (future) category based on observed data \rightarrow classification
- prediction of a (future) numerical value y based on observed data \vec{x}
 - y: response output, dependent variable
 - \vec{x} : input, regressors, explanatory variables, independent variables
- applications
 - the output is expensive to measure, the input not
 - the value of the inputs is known before the value of the output and a prediction is required
 - simulation of system behaviour by controlling the inputs
 - detecting causal links between the inputs and the output

• most common form: linear regression

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 - · assuming a linar function

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• inserting all m training samples $\rightarrow m$ new equations

$$y_i = \epsilon_j + a_{0j} + \sum_{i=1}^n a_i \cdot x_{ij}$$

 $\epsilon_j (j = 1 \dots m)$: regression error for each given sample

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 $\epsilon_j (j=1\dots m)$: regression error for each given sample

• modify the linear coefficients a_i to minimize the sum of error squares $e = \sum_{i=1}^n \epsilon_i^2$

special case: single predictor variable

$$y = f(x) = a_0 + a_1 \cdot x$$

$$e = \sum_{i=1}^{n} \epsilon_i^2 = \sum_{i=1}^{n} (y_i - y_i')^2 = \sum_{i=1}^{n} (y_i - a_0 - a_1 x_i)^2$$

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minimizing for a₀ and a₁

$$\frac{\delta e}{\delta a_0} = -2\sum_{i=1}^n (y_i - a_0 - a_1 x_i) = 0$$

$$\frac{\delta e}{\delta a_1} = -2 \sum_{i=1}^{n} (y_i - a_0 - a_1 x_i) \cdot x_i = 0$$

minimizing (cont.)

$$a_0 + a_1 \sum_{i=1}^{n} x_i = \sum_{i=1}^{n} y_i$$

$$a_0 \sum_{i=1}^{n} x_i + a_1 \sum_{i=1}^{n} x_i^2 = \sum_{i=1}^{n} x_i y_i$$

$$a_0 = \mu_y - a_1 \mu_x$$

$$a_1 = \frac{\sum_{i=1}^{n} (x_i - \mu_x) \cdot (y_i - \mu_y)}{\sum_{i=1}^{n} (x_i - \mu_x)^2}$$

multiple regression (multiple predictor variables)

$$y = a_0 + \vec{a} \cdot \vec{x}$$
$$e = (\vec{y} - a_0 \vec{a} \cdot \vec{X})^T \cdot (\vec{y} - a_0 \vec{a} \cdot \vec{X})$$

X: Matrix of all data vectors $\vec{x_i}$ from the training set

$$\vec{a} = (X^T \cdot X)^{-1}(X^T \cdot \vec{y})$$

- solution of equation set requires exponential effort
- not feasible for realistic training sets

- identifying the relevant variables
 - selectively add to or delete variables from an initial set
 - testing for a linear relationship: correlation

$$r = \frac{\sum_{i=1}^{n} (x_i - \mu_x) \cdot (y_i - \mu_y)}{\sqrt{\sum_{i=1}^{n} (x_i - \mu_x) \cdot \sum_{i=1}^{n} (y_i - \mu_y)}}$$

- non-linear relationships
 - transform to a linear equation

polynomial	$y = ax^2 + bx + c$	$x^* = x^2$
exponential	$y = ae^{bx}$	$y^* = \ln y$
power	$y = ax^b$	$y^* = \log y, x^* = \log x$
reciprocal	$y = a + b\frac{1}{x}$	$x^* = \frac{1}{x}$
hyperbolic	$y = \frac{x}{a+bx}$	$y^* = \frac{1}{y}, x^* = \frac{1}{x}$

- non-linear relationships
 - transform to a linear equation

$$\begin{array}{lll} \text{polynomial} & y = ax^2 + bx + c & x^* = x^2 \\ \text{exponential} & y = ae^{bx} & y^* = \ln y \\ \text{power} & y = ax^b & y^* = \log y, x^* = \log x \\ \text{reciprocal} & y = a + b\frac{1}{x} & x^* = \frac{1}{x} \\ \text{hyperbolic} & y = \frac{x}{a+bx} & y^* = \frac{1}{y}, x^* = \frac{1}{x} \end{array}$$

- use neural networks to approximate a nonlinear function \rightarrow low perspicuity

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- grouping of data points according to their inherent structure
 - based on a similarity measure
 - learning without teacher

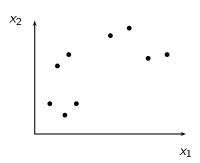
- grouping of data points according to their inherent structure
 - based on a similarity measure
 - learning without teacher
- many clustering approaches
 - agglomerative clustering
 - · partitioning clustering
 - incremental clustering
 - clustering with neural networks

• computing the optimal clustering is computationally infeasible

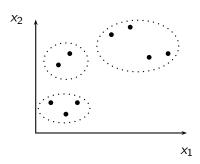
ightarrow greedy, sub-optimal approaches

- \bullet computing the optimal clustering is computationally infeasible \to greedy, sub-optimal approaches
- different clustering algorithms might lead to different clustering results

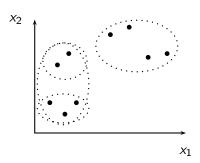
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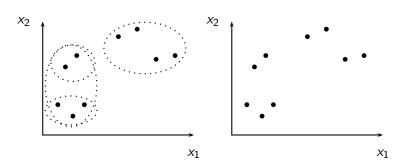
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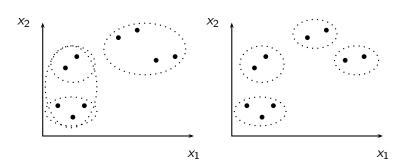
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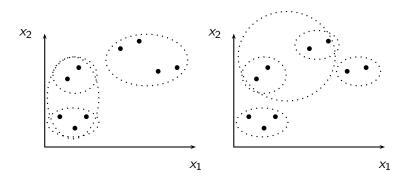
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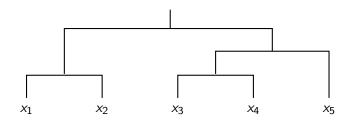


• agglomerative/hierarchical clustering

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- successively merging data sets

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- result can be displayed as a dendrogram

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- successively merging data sets
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- algorithm
 - initially each cluster consists of a single data point
 - determine all inter-cluster distances
 - · merge the least distant clusters into a new one
 - continue until all clusters have been merged

Distance Measures

- distance measure for clusters
 - single link: minimum of distances between all pairs of data points
 - complete link: e.g. mean of distances between all pairs of data points

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- distance measure for clusters
 - single link: minimum of distances between all pairs of data points
 - complete link: e.g. mean of distances between all pairs of data points
- local clustering criterion for data points: minimal mutual neighbor distance (MND)
 - distance depends also on the local context of a data point

$$d_{MND}(\vec{x_i}, \vec{x_j}) = r(\vec{x_i}, \vec{x_j}) + r(\vec{x_j}, \vec{x_i})$$

 $r(\vec{x_i}, \vec{x_j})$: rank of x_j according to distance from x_i

Partitioning Clustering

mutual neighbor distance (MND)

$$d_{MND}(A, B) = r(A, B) + r(B, A)$$

= 1 + 1 = 2
 $d_{MND}(B, C) = r(B, C) + r(C, B)$
= 2 + 1 = 3

$$d_{MND}(A, B) = r(A, B) + r(B, A)$$

$$= 3 + 3 = 6$$

$$d_{MND}(B, C) = r(B, C) + r(C, B)$$

$$= 4 + 1 = 5$$

$$C$$

$$B$$

$$E$$

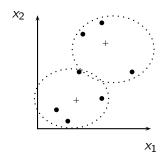
Data Mining

Partitioning Clustering

• number of resulting clusters is given in advance

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- each cluster is represented by a centroid

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- global clustering criterion: minimizing the mean square error
 - mean vector as centroid

$$\vec{c_k} = \frac{1}{n_k} \sum_{i=1}^{n_k} \vec{x_{ik}}$$

error for one cluster (within-cluster variation)

$$e_k^2 = \sum_{i=1}^{n_k} (\vec{x_{ik}} - \vec{c_k})^2$$

• global error
$$e = \sum_{k=1}^{K} e_k^2$$

- algorithm for k-means partitioning clustering
 - select a randomly chosen initial partitioning with k clusters
 - compute the centroids
 - assign each sample to the nearest centroid
 - compute new centroids
 - continue until the clustering stabilizes (or another termination criterion based on the global error is met)
- see Section Data Preparation: Number of Values Reduction

- huge data sets cannot be clustered in a single step
 - · divide-and-conquer: cluster subsets and merge the results
 - incremental clustering: data points are loaded successively and the cluster representation is updated accordingly

- algorithm
 - assign the first data point to the first cluster
 - consider the next data point
 - assign it to an already existing cluster, or
 - create a new cluster
 - · recompute the cluster description for that cluster
 - continue until all data points are clustered

- cluster description
 - centroid
 - number of data points in the cluster
 - "radius" of the cluster (based on the mean-squared distance to the centroid)

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- problems
 - result depends on the order in which data points are processed
 - ightarrow iterative incremental clustering
 - use the centroids of the previous iteration for partitioning in the next one

· competitive learning

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 - single layer network
 - each output neuron corresponds to a cluster
 - the neurons are coupled: lateral inhibition
 - the output of the neuron with maximum activation is set to one;

all other to zero

$$y_k' = \left\{ \begin{array}{ll} 1 & \text{if } y_k > y_j \ \forall j \ . \ j \neq k \\ 0 & \text{else} \end{array} \right.$$

 the weights of the inputs of the winning neuron are adjusted as to move them towards the observed sample

$$w'_{ij} = \left\{ egin{array}{ll} w_{ij} + \eta(x_i - w_{ij}) & ext{for the winning neuron} \ w_{ij} & ext{else} \end{array}
ight.$$

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 overall effect: moving the weights towards the center of gravity of the corresponding cluster

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- other neural network approaches
 - self-organizing maps (SOM)
 - learning vector quantization (LVQ)

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 - placement of items in a store
 - layout of mail-order catalogues
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• finding good combinations of premises is a combinatorial problem

• example data base:

trans-	item
action	
001	cola
001	chips
001	peanuts
002	beer
002	chips
002	cigarettes

trans-	items
action	
001	{chips, cola, peanuts}
002	{beer, chips, cigarettes}
003	{beer, chips, cigarettes, cola}
004	{beer, cigarettes}

• set of n different items $I = \{x_j | j = 1, \dots, n\}$

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- data base: $D = \{(k, T_k) | k = 1, ..., m\}$

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- data base: $D = \{(k, T_k) | k = 1, ..., m\}$
- support of an itemset: share of transactions which contain the itemset

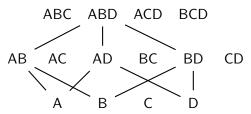
$$s(I_i) = \frac{|\{T_k|I_i \subseteq T_k\}|}{|D|}$$

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- i-itemset: $I_k^i \subseteq I$, $|I_k^i| = i$
- transaction $T_k \subseteq I$
- data base: $D = \{(k, T_k) | k = 1, ..., m\}$
- support of an itemset: share of transactions which contain the itemset

$$s(I_i) = \frac{|\{T_k|I_i \subseteq T_k\}|}{|D|}$$

• frequent (strong, large) itemset: $s(I_i) \ge s_{min}$

 downward closure: every subset of a frequent itemset is also a frequent itemset



 every superset of a not frequent itemset is also a not frequent itemset

• association rule: $X \to Y$, $X, Y \subseteq I, Y \cap X = \emptyset$

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- support of a rule: share of transactions which contain both, premise and conclusion of the rule

$$s(X \to Y) = s(X \cup Y) = \frac{|\{T_k | X \cup Y \subseteq T_k\}|}{|D|} = p(XY)$$

- association rule: $X \to Y$, $X, Y \subseteq I, Y \cap X = \emptyset$
- support of a rule: share of transactions which contain both, premise and conclusion of the rule

$$s(X \to Y) = s(X \cup Y) = \frac{|\{T_k | X \cup Y \subseteq T_k\}|}{|D|} = p(XY)$$

 confidence of a rule: share of transactions supporting the rule from those supporting the premise

$$c(X \to Y) = \frac{s(X \cup Y)}{s(X)} = \frac{|\{T_k | X \cup Y \subseteq T_k\}|}{|\{T_k | X \subseteq T_k\}|} = p(Y | X)$$

• strong rule: high support + high confidence

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- detection of strong rules: two pass algorithm
- 1. find frequent (strong, large) itemsets (Apriori)
 - necessary to generate rules with strong support
 - uses the downward closure
 - itemsets are ordered

- strong rule: high support + high confidence
- detection of strong rules: two pass algorithm
- 1. find frequent (strong, large) itemsets (Apriori)
 - necessary to generate rules with strong support
 - uses the downward closure
 - itemsets are ordered
- 2. use the frequent itemsets to generate association rules
 - find strong correlations in a frequent itemset

- Apriori: finding frequent itemsets of increasing size itemsets are ordered!
 - start with all itemsets of size one: I^1
 - select all itemsets with sufficient support
 - from the selected itemsets I^i generate larger itemsets I^{i+1}

$$is(\{i_1, \dots, i_{n-2}, i_{n-1}\}) \wedge is(\{i_1, \dots, i_{n-2}, i_n\})$$

 $\rightarrow is(\{i_1, \dots, i_{n-2}, i_{n-1}, i_n\})$

- already blocks some of the non-frequent itemsets, but not all of them
- remove those itemsets which still contain a non-frequent immediate subset
 - they cannot have enough support (downward closure)
- continue until no further frequent itemsets can be generated

- example data base again
- assumption: minimum support $s_{min} = 0.5$

k	T_k	I_k^1	#	$s(I_k^1)$
001	{chips, cola, peanuts}	{chips}		
002	{beer, chips, cigarettes}	{cola}		
003	{beer, chips, cigarettes, cola}	{peanuts}		
004	{beer, cigarettes}	{beer}		
		{cigarettes}		

- example data base again
- assumption: minimum support $s_{min} = 0.5$

k	T_k	I_k^1	#	$s(I_k^1)$
001	{chips, cola, peanuts}	{chips}		
002	{beer, chips, cigarettes}	{cola}		
003	{beer, chips, cigarettes, cola}	$\{peanuts\}$		
004	{beer, cigarettes}	{beer}		
	·	{cigarettes}		

no non-empty subsets

- example data base again
- assumption: minimum support $s_{min} = 0.5$

k	T_k	I_k^1	#	$s(I_k^1)$
001	{chips, cola, peanuts}	{chips}	3	0.75
002	{beer, chips, cigarettes}	$\{cola\}$	2	0.5
003	{beer, chips, cigarettes, cola}	$\{peanuts\}$	1	0.25
004	{beer, cigarettes}	{beer}	3	0.75
		{cigarettes}	3	0.75

no non-empty subsets

- example data base again
- assumption: minimum support $s_{min} = 0.5$

k	T_k	I_k^1	#	$s(I_k^1)$
001	{chips, cola, peanuts}	{chips}	3	0.75
002	{beer, chips, cigarettes}	{cola}	2	0.5
003	{beer, chips, cigarettes, cola}	$\{peanuts\}$	1	0.25
004	{beer, cigarettes}	{beer}	3	0.75
	·	{cigarettes}	3	0.75

no non-empty subsets

I_k^1	#	$s(I_k^1)$
{chips}	3	0.75
$\{cola\}$	2	0.5
$\{beer\}$	3	0.75
{cigarettes}	3	0.75

I_k^2	#	$s(I_k^2)$
{chips, cola}		
{beer, chips}		
{chips, cigarettes}		
$\{beer,cola\}$		
{cigarettes, cola}		
{beer, cigarettes}		

• 2-itemsets I_k^2

I_k^1	#	$s(I_k^1)$	I_k^2	#	$s(I_k^2)$
{chips}	3	0.75	{chips, cola}		
$\{cola\}$	2	0.5	{beer, chips}		
{beer}	3	0.75	{chips, cigarettes}		
{cigarettes}	3	0.75	{beer, cola}		
			{cigarettes, cola}		
			{beer, cigarettes}		

• no itemsets to prune

I_k^1	#	$s(I_k^1)$
{chips}	3	0.75
$\{cola\}$	2	0.5
$\{beer\}$	3	0.75
{cigarettes}	3	0.75

I_k^2	#	$s(I_k^2)$
{chips, cola}	2	0.5
$\{beer,chips\}$	2	0.5
{chips, cigarettes}	2	0.5
$\{beer,cola\}$	1	0.25
{cigarettes, cola}	1	0.25
{beer, cigarettes}	3	0.75

I_k^1	#	$s(I_k^1)$
{chips}	3	0.75
$\{cola\}$	2	0.5
{beer}	3	0.75
$\{cigarettes\}$	3	0.75

I_k^2	#	$s(I_k^2)$
{chips, cola}	2	0.5
{beer, chips}	2	0.5
{chips, cigarettes}	2	0.5
$\{beer, cola\}$	1	0.25
{cigarettes, cola}	1	0.25
{beer, cigarettes}	3	0.75

I_k^2	#	$s(I_k^2)$
{chips, cola}	2	0.5
$\{beer,chips\}$	2	0.5
{chips, cigar.}	2	0.5
{beer, cigar.}	3	0.75

I_k^3	#	$s(I_k^2)$
{beer, chips, cigar.}		
{chips, cigar., cola}		

I_k^2	#	$s(I_k^2)$
{chips, cola}	2	0.5
$\{beer,chips\}$	2	0.5
{chips, cigar.}	2	0.5
{beer, cigar.}	3	0.75

I_k^3	#	$s(I_k^2)$
{beer, chips, cigar.}		
{chips, cigar., cola}		

I_k^2	#	$s(I_k^2)$
{chips, cola}	2	0.5
{beer, chips}	2	0.5
{chips, cigar.}	2	0.5
{beer, cigar.}	3	0.75

I_k^3	#	$s(I_k^2)$
{beer, chips, cigar.}		
{chips, cigar., cola}		

I_k^2	#	$s(I_k^2)$
{chips, cola}	2	0.5
$\{beer,\;chips\}$	2	0.5
{chips, cigar.}	2	0.5
{beer, cigar.}	3	0.75

I_k^3	#	$s(I_k^2)$
{beer, chips, cigar.}	2	0.5
{chips, cigar., cola}		

#	$s(I_k^2)$
2	0.5
2	0.5
2	0.5
3	0.75
	2 2

I_k^3	#	$s(I_k^2)$
{beer, chips, cigar.}	2	0.5
{chips, cigar., cola}		

#	$s(I_k^2)$
2	0.5
2	0.5
2	0.5
3	0.75
	2 2

I_k^3	#	$s(I_k^2)$
{beer, chips, cigar.}	2	0.5
{chips, cigar., cola}	1	0.25

resulting frequent itemsets:

```
{beer, chips, cigarettes}
{chips, cola}
{chips, beer}
{chips, cigar.}
{beer, cigar.}
{beer}
{chips}
{chips}
{cola}
```

- generation of strong association rules:
 - for all frequent itemsets I_j determine all nonempty subsets I_k for which

$$c = \frac{s(I_j)}{s(I_k)} \ge c_{min}$$

• add a rule $I_k \to Y$, $Y = I_j - I_k$ to the rule set

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- add a rule $I_k \to Y$, $Y = I_j I_k$ to the rule set
- e.g. $s(\{chips\}) = 0.75, s(\{cola\}) = 0.5, s(\{chips, cola\}) = 0.5$

rule	confidence
	1.00
$\{chips\} \to \{cola\}$	0.67

• interesting association rules: only those for which the confidence is greater than the support of the conclusion

$$c(X \rightarrow Y) > s(Y)$$

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$$c(X \rightarrow Y) > s(Y)$$

negative border:

$$\{I_k \mid s(I_k) < s_{min} \land \forall I_j \subset I_k : s(I_j) \geq s_{min}\}$$

used

- to compute the set of frequent itemsets more efficiently
- to derive negative association rules

- Apriori: number of potential itemsets is exponential in the number of items
- but:
 - data is sparse: $|T_i| \ll |I|$
 - itemsets are generated in separate scans of the data base
 - · size of generated itemsets grows monotonically
 - large itemsets are useless
 - only k scans required $(k \ll |I|)$

- modifications / extensions
 - rule mining on relational data
 - Apriori for hierarchically organised items
 - 2-scan Apriori
 - sampled transactions
 - · incremental rule mining
 - non uniform support thresholds
 - class association rules
 - (mining sequential data)

Relational Data

- relational data has to be transformed into transaction data
- ullet Apriori requires categorical data o binning has to be performed
- the same category can appear as value of different attributes

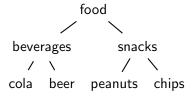
age	income	debt
low	low	low
middle	low	high
high	high	low

- values have to be combined with their attribute
 - attribute-value pairs are taken as items

1	(age, low)	(income, low)	(debt, low)
2	(age, middle)	(income, low)	(debt, high)
3	(age, high)	(income, high)	(debt, low)

Hierarchical Apriori

• in addition to the base level of items, determine also frequent itemsets on a higher level in an is-a hierarchy



sometimes regularities can only be found at higher levels of abstraction

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- partitioned Apriori: two scans
 - 1st scan: partition the database and compute locally frequent itemsets on the partitions
 - 2nd scan: determine the support of all locally frequent itemsets
 - heuristics: if an itemset is globally frequent it will be so locally in at least one partition
 - \rightarrow second scan deals with a superset of possible itemsets

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 - 1st scan: take a sample and compute frequent itemsets
 - 2nd scan: count their support and the support for their immediate supersets
 - if the itemset is at the negative border
 - all frequent itemsets have been found
 - else check supersets of the itemsets for being at the negative border in subsequent scans

Incremental Rule Mining

- incremental update: scan only the added transactions, whether they
 - invalidate a former frequent itemset, or
 - introduce new frequent itemsets

Non-uniform Support Thresholds

- items differ in their frequency of occurrence in the data base
- solution (1): using a single minimum support threshold s_{min}
- problem: using a single threshold disfavors rare items
 - minimum support too high: itemsets containing rare items cannot be found
 - minimum support too low: too many itemsets are found (combinatorial explosion)
- associations with rare items might be particularly interesting

Non-uniform Support Thresholds

- solution (2):
 - ullet assigning individual thresholds s_{min}^i to the items
 - but preventing the generation of itemsets with extremely different thresholds

$$\max_{i \in I_k} s_{min}^i - \min_{i \in I_k} s_{min}^i < \delta$$

 δ : global maximum support difference

- assigning a threshold $s_{min}^{i} > 1$ excludes an item from consideration
 - can be used to guide the mining process towards the interesting items
- support of an itemset has to be replaced by its minimum support:

$$s_{min}(I_k) = \min_{i \in I_k} s_{min}^i$$

Non-uniform Support Thresholds

- problem: downward closure property does not hold any longer
 - minimum support of an itemset is no longer monotonic

$$I_k \subset I_l \to s_{min}(I_k) < s_{min}(I_l)$$

- adding an item to an itemset might decrease its minimum support
- an itemset might be frequent, while one of its subsets is not
- · itemset generation
 - sort the items in the itemsets according to their minimum support values s_{min}^i
 - a frequent itemset I_k needs not be extended by an item with a lower minimum support $s_{min}^i < s_{min}(I_k)$
- rule generation
 - if $ab \rightarrow c$ is a rule with sufficient confidence $a \rightarrow bc$, or $b \rightarrow ac$ need not be
 - support values for all subsets of frequent itemsets have to be recorded

Class Association Rules

- so far: any item or combination of them can appear in the consequence part of a rule
- now: associations to a fixed target item required
- rules of the form

$$\{i_1,...,i_n\} \rightarrow c_j, i_i \in I, c_j \in C, C \cap I = \emptyset$$

- can be used used for classification
 - texts
 - · search queries,
 - ...

Class Association Rules

- ruleitem: (condset,c)
- support and confidence defined as usual
 - support for the condition: $s_c = s(condset)$
 - support for a rule: $s_r = s(condset \cup c)$
 - confidence of a rule: $c_r = s_r/s_c$
- similar algorithm: multiple scans with a growing number of items in the condition of the rule
- redundant rules: if a rule has a confidence of 1, each rule generated from it will also have a confidence of 1
 - should be avoided
- extension to relational data and non-uniform support thresholds possible

Data Mining Tasks

- Classification
- Prediction
- Clustering
- Dependency Modelling
- Summarization
- Change and Deviation Detection
- Visualization

Summarization

extraction of representative information about the database

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- simple descriptions: characterizations, generalizations

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- extraction of representative information about the database
- simple descriptions: characterizations, generalizations
 - point estimations: mean, variance
 - confidence intervals
 - regression functions
 - cluster with prototypical examples
 - association rules

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- transaction time databases: tuples or attribute values are timestamped when inserted
- valid time databases: tuples or attribute values can be annotated for the time range in which they are valid
- bitemporal databases: both types of temporal information are supported

Sequential Structures

- time is inherently sequential
- models for capturing sequential structures
 - Finite State Automata
 - Markov Models
 - Hidden Markov Models

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- time is inherently sequential
- models for capturing sequential structures
 - Finite State Automata
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 - Hidden Markov Models
- all require supervised training

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- outlier detection: not only global outliers but also outliers in a local context

- longest common subsequence
 - fraud detection
 - genomic analysis
 - failure prediction
 - desaster prediction (vulcano eruptions, earthquakes, floodings)

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- longest common subsequence
 - fraud detection
 - · genomic analysis
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 - desaster prediction (vulcano eruptions, earthquakes, floodings)
- for categorial data: extension of Apriori to sequences
- flexible match required
 - extension of the similarity measures to sequences, e.g.
 LEVENSHTEIN-metric (elastic match, dynamic time warping)
 - general case: match with transpositions
- for numerical data: (Hidden) Markov Models

- in some applications the order of items is relevant: click streams, natural language text, repeated shopping
- extension of Apriori to sequences of itemsets

$$\langle e_1,...,e_n\rangle$$
, with $e_i\subseteq I$

• items in the elements are lexicographically ordered (as in Apriori)

size of a sequence: number of itemsets it contains

$$size(s) = |s|$$

 $size(\langle \{2\}, \{3, 5\}, \{1, 4\} \rangle) = 3$

• length of a sequence: number of elements in the sequence

$$length(s) = \sum_{i=1}^{n} e_i$$
, with $n = size(s)$

$$length(\langle \{2\}, \{3,5\}, \{1,4\} \rangle) = 5$$

• subsequence/supersequence:

```
s_1=\langle a_1,a_2,...,a_n \rangle is a subsequence of s_2=\langle b_1,b_2,...,b_m \rangle (s_2 contains s_1), if there exists intergers 1 \leq j_1 \leq j_2 \leq ... \leq j_o \leq m so that a_1 \subseteq b_{j_1}, a_2 \subseteq b_{j_2},...,a_n \subseteq b_{j_o}
```

 support of a sequence: fraction of data sequences which contain the sequence

customer	date	transaction
1	2012/06/13	30
1	2012/06/19	90
2	2012/06/03	10, 20
2	2012/06/09	30
2	2012/06/16	10, 40, 60, 70
3	2012/06/16	30, 50, 70, 80
4	2012/06/05	30
4	2012/06/05	30, 40, 70, 80
4	2012/06/05	90
5	2012/06/19	90

customer	transaction sequence	
1	$\langle \{30\}, \{90\} \rangle$	
2	$\langle \{10, 20\}, \{30\}, \{10, 40, 60, 70\} \rangle$	
3	$\langle \{30, 50, 70, 80\} \rangle$	
4	$\langle \{30\}, \{30, 40, 70, 80\}, \{90\} \rangle$	
5	$\langle \{90\} \rangle$	

customer	transaction sequence	
1	$\langle \{30\}, \{90\} \rangle$	
2	$\langle \{10, 20\}, \{30\}, \{10, 40, 60, 70\} \rangle$	
3	$\langle \{30, 50, 70, 80\} \rangle$	
4	$\langle \{30\}, \{30, 40, 70, 80\}, \{90\} \rangle$	
5	$\langle \{90\} \rangle$	

length	sequential patterns with $s \geq 0.25$
1	$\langle \{30\} \rangle, \langle \{40\} \rangle, \langle \{70\} \rangle, \langle \{80\} \rangle, \langle \{90\} \rangle$
2	$\langle \{30\}, \{40\} \rangle, \langle \{30\}, \{70\} \rangle, \langle \{30\}, \{90\} \rangle,$
	$\langle \{30,70\} \rangle, \langle \{30,80\} \rangle, \langle \{40,70\} \rangle, \langle \{70,80\} \rangle$
3	$\langle \{30\}, \{40, 70\} \rangle, \langle \{30\}, \{70\}, \{80\} \rangle$

- can be extended to non-uniform minimum support
- sequential rules: $X \to Y$ with Y being a sequence and X a proper subsequence of Y
- useful rules
 - rules with wildcard symbols (label sequence rules)
 - wildcard symbols usually increase the confidence for a sequence
 - predict unseen/missing elements in a data sequence

$$\langle \{1\}, \{*\}, \{7, *\} \rangle \to \langle \{1\}, \{3\}, \{7, 8\} \rangle$$

• class sequential rules

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Visualization

- seeing is the construction of a mental image
 - abstraction: identification of objects, assigning properties
 - generalization: summarized information about many data points

Visualization

- seeing is the construction of a mental image
 - abstraction: identification of objects, assigning properties
 - generalization: summarized information about many data points
- basic graph types
 - bar charts
 - histograms (distributions)
 - line charts
 - pie charts
 - scatter plots

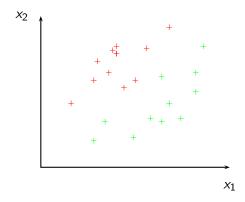
Visualization

- problem: limited dimensionality
 - two (three) basic dimensions
 - overlay of multiple graphs
 - color
 - texture
 - shape
 - animation

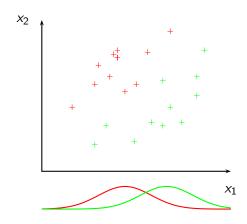
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 - two (three) basic dimensions
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- combination of visualisation techniques with data cube operations
- interactive exploration of data: browsing

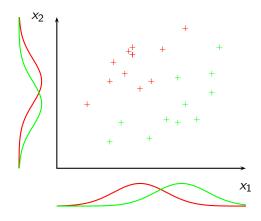
rolling the dice is not always sufficient



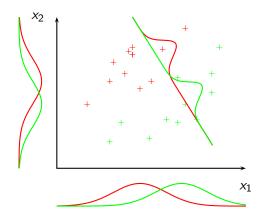
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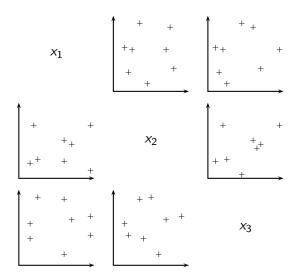


Multi-Dimensional Visualization

- scatter-plot matrix
- parameter stacks
- parallel coordinates
- star display
- radial visualization

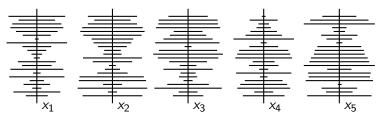
Scatter-Plot Matrix

n × n-matrix of all combinations of two dimensions



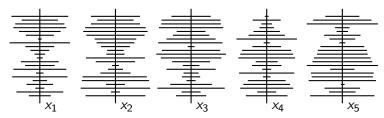
Parameter Stacks

data plots on vertical lines as centered horizontal lines



Parameter Stacks

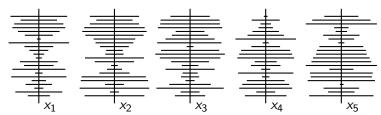
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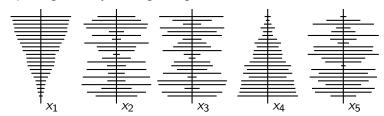
• exploring data by sorting along a dimension

Parameter Stacks

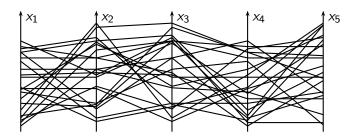
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exploring data by sorting along a dimension



Parallel Coordinates



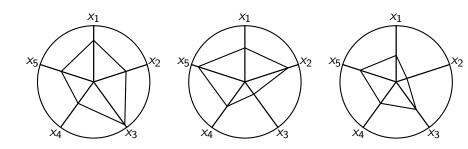
- exploring data by investigating neighborhood relationships between dimensions
 - rearranging

Star Display

• radial version of parallel coordinates

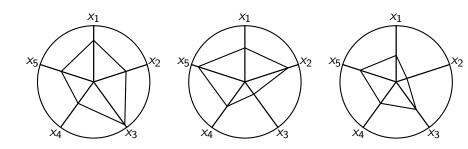
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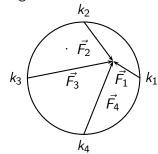
Star Display

radial version of parallel coordinates



• only for the display of few data points

- attraction-based: forces proportional to the n dimensions pull the point towards the dimension anchors
- equilibrium: forces must sum up to 0
- mapping the *n*-dimensional space into a two dimensional one $(k_1, k_2, k_3, k_4, ..., k_n) \mapsto (x, y)$
- e.g. n = 4



$$\vec{F_1} + \vec{F_2} + \vec{F_3} + \vec{F_4} = 0$$

$$k_{1} \begin{pmatrix} 1-x \\ 0-y \end{pmatrix} + k_{2} \begin{pmatrix} 0-x \\ 1-y \end{pmatrix} + k_{3} \begin{pmatrix} -1-x \\ 0-y \end{pmatrix} + k_{4} \begin{pmatrix} 0-x \\ -1-y \end{pmatrix} = 0$$

$$k_{1} - k_{1} \cdot x - k_{2} \cdot x - k_{3} - k_{3} \cdot x - k_{4} \cdot x = 0$$

$$-k_{1} \cdot y + k_{2} - k_{2} \cdot y - k_{3} \cdot y - k_{4} - k_{4} \cdot x = 0$$

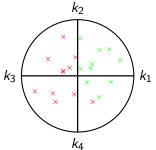
$$k_{1} - k_{3} - x(k_{1} + k_{2} + k_{3} + k_{4}) = 0$$

$$k_{2} - k_{4} - y(k_{1} + k_{2} + k_{3} + k_{4}) = 0$$

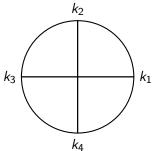
$$x = \frac{k_{1} - k_{3}}{k_{1} + k_{2} + k_{3} + k_{4}}$$

$$y = \frac{k_2 - k_4}{k_1 + k_2 + k_3 + k_4}$$

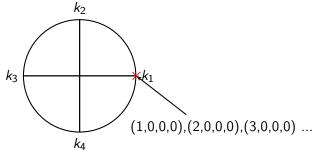
• important spacial relationships are preserved: e.g. class separation



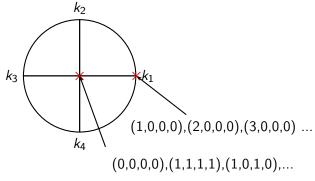
• information loss: lines are mapped to points



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- · hearing data
- auditory channel is inherently multidimensional
 - volume, rhythm, pitch, harmony, polyphony, sound color, ...

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 - volume, rhythm, pitch, harmony, polyphony, sound color, ...
- approaches
 - audification
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 - model-based sonification

- audification: direct mapping of time-series data to sound patterns
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- sound mapping: controlling sound synthesis parameter by data items
 - · high-dimensional data can be presented
- model-based sonification: excitation of an oscillating model by data items
 - energetically coupled particles, growing neural gas
 - interactive exploration of the (auditory) system response
 - linear structures in a high-dimensional space can be identified